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In[1]:= Quartic@x_, y_, z_D = a0*x^4 + a1*x^3*y + a2*x^3*z + a3*x^3 + a4*x^2*y^2 +
a5*x^2*y*z + a6*x^2*y + a7*x^2*z^2 + a8*x^2*z + a9*x^2 +
a10*x*y^3 + a11*x*y^2*z + a12*x*y^2 + a13*x*y*z^2 + a14*x*y*z +
a15*x*y + a16*x*z^3 + a17*x*z^2 + a18*x*z + a19*x +
a20*y^4 + a21*y^3*z + a22*y^3 + a23*y^2*z^2 + a24*y^2*z +
a25*y^2 + a26*y*z^3 + a27*y*z^2 + a28*y*z + a29*y +
a30*z^4 + a31*z^3 + a32*z^2 + a33*z + a34
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Out[1]= x^4 a0 + x^3 y a1 + x^3 z a2 + x^3 a3 + x^2 y^2 a4 + x^2 y z a5 + x^2 y a6 + x^2 z^2 a7 +
x^2 z a8 + x^2 a9 + x y^3 a10 + x y^2 z a11 + x y^2 a12 + x y z^2 a13 + x y z a14 + x y a15 +
x z^3 a16 + x z^2 a17 + x z a18 + x a19 + y^4 a20 + y^3 z a21 + y^3 a22 + y^2 z^2 a23 + y^2 z a24 +
y^2 a25 + y z^3 a26 + y z^2 a27 + y z a28 + y a29 + z^4 a30 + z^3 a31 + z^2 a32 + z a33 + a34

x^4 a0 + x^3 y a1 + x^3 z a2 + x^3 a3 + x^2 y^2 a4 + x^2 y z a5 + x^2 y a6 + x^2 z^2 a7 +
x^2 z a8 + x^2 a9 + x y^3 a10 + x y^2 z a11 + x y^2 a12 + x y z^2 a13 + x y z a14 + x y a15 +
x z^3 a16 + x z^2 a17 + x z a18 + x a19 + y^4 a20 + y^3 z a21 + y^3 a22 + y^2 z^2 a23 + y^2 z a24 +
y^2 a25 + y z^3 a26 + y z^2 a27 + y z a28 + y a29 + z^4 a30 + z^3 a31 + z^2 a32 + z a33 + a34
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In[2]:= **CollectAQuartic@s<sub>x</sub> + c<sub>x</sub>\*t, s<sub>y</sub> + c<sub>y</sub>\*t, s<sub>z</sub> + c<sub>z</sub>\*tD, 9t<sup>0</sup>, t<sup>1</sup>, t<sup>2</sup>, t<sup>3</sup>, t<sup>4</sup>=E**

$$\begin{aligned}
 Out[2]= & a_{34} + t^4 H a_0 c_x^4 + a_1 c_x^3 c_y + a_4 c_x^2 c_y^2 + a_{10} c_x c_y^3 + a_{20} c_y^4 + a_2 c_x^3 c_z + a_5 c_x^2 c_y c_z + \\
 & a_{11} c_x c_y^2 c_z + a_{21} c_y^3 c_z + a_7 c_x^2 c_z^2 + a_{13} c_x c_y c_z^2 + a_{23} c_y^2 c_z^2 + a_{16} c_x c_z^3 + a_{26} c_y c_z^3 + a_{30} c_z^4 L + \\
 & a_{19} s_x + a_9 s_x^2 + a_3 s_x^3 + a_0 s_x^4 + a_{29} s_y + a_{15} s_x s_y + a_6 s_x^2 s_y + a_1 s_x^3 s_y + a_{25} s_y^2 + a_{12} s_x s_y^2 + \\
 & a_4 s_x s_y^2 + a_{22} s_x^3 + a_{10} s_x s_y^3 + a_{20} s_y^4 + a_{33} s_z + a_{18} s_x s_z + a_8 s_x^2 s_z + a_2 s_x^3 s_z + a_{28} s_y s_z + \\
 & a_{14} s_x s_y s_z + a_5 s_x s_y s_z + a_{24} s_y^2 s_z + a_{11} s_x s_y^2 s_z + a_{21} s_y^3 s_z + a_{32} s_z^2 + a_{17} s_x s_z^2 + \\
 & a_7 s_x^2 s_z^2 + a_{27} s_y s_z^2 + a_{13} s_x s_y s_z^2 + a_{23} s_y^2 s_z^2 + a_{31} s_z^3 + a_{16} s_x s_z^3 + a_{26} s_y s_z^3 + a_{30} s_z^4 + \\
 & t^3 H a_3 c_x^3 + a_6 c_x^2 c_y + a_{12} c_x c_y^2 + a_{22} c_y^3 + a_8 c_x^2 c_z + a_{14} c_x c_y c_z + a_{24} c_y^2 c_z + a_{17} c_x c_z^2 + \\
 & a_{27} c_y c_z^2 + a_{31} c_z^3 + 4 a_0 c_x^3 s_x + 3 a_1 c_x^2 c_y s_x + 2 a_4 c_x c_y^2 s_x + a_{10} c_y^3 s_x + 3 a_2 c_x^2 c_z s_x + \\
 & 2 a_5 c_x c_y c_z s_x + a_{11} c_y^2 c_z s_x + 2 a_7 c_x c_z^2 s_x + a_{13} c_y c_z^2 s_x + a_{16} c_z^3 s_x + a_1 c_x^3 s_y + \\
 & 2 a_4 c_x^2 c_y s_y + 3 a_{10} c_x c_y^2 s_y + 4 a_{20} c_y^3 s_y + a_5 c_x^2 c_z s_y + 2 a_{11} c_x c_y c_z s_y + 3 a_{21} c_y^2 c_z s_y + \\
 & a_{13} c_x c_z^2 s_y + 2 a_{23} c_y c_z^2 s_y + a_{26} c_z^3 s_y + a_2 c_x^3 s_z + a_5 c_x^2 c_y s_z + a_{11} c_x c_y^2 s_z + a_{21} c_y^3 s_z + \\
 & 2 a_7 c_x^2 c_z s_z + 2 a_{13} c_x c_y c_z s_z + 2 a_{23} c_y^2 c_z s_z + 3 a_{16} c_x c_z^2 s_z + 3 a_{26} c_y c_z^2 s_z + 4 a_{30} c_z^3 s_z L + \\
 & t^2 H a_9 c_x^2 + a_{15} c_x c_y + a_{25} c_y^2 + a_{18} c_x c_z + a_{28} c_y c_z + a_{32} c_z^2 + 3 a_3 c_x^2 s_x + 2 a_6 c_x c_y s_x + \\
 & a_{12} c_y^2 s_x + 2 a_8 c_x c_z s_x + a_{14} c_y c_z s_x + a_{17} c_x^2 s_x + 6 a_0 c_x^2 s_x^2 + 3 a_1 c_x c_y s_x^2 + a_4 c_y^2 s_x^2 + \\
 & 3 a_2 c_x c_z s_x^2 + a_5 c_y c_z s_x^2 + a_7 c_z^2 s_x^2 + a_6 c_x^2 s_y + 2 a_{12} c_x c_y s_y + 3 a_{22} c_y^2 s_y + a_{14} c_x c_z s_y + \\
 & 2 a_{24} c_y c_z s_y + a_{27} c_z^2 s_y + 3 a_1 c_x^2 s_x s_y + 4 a_4 c_x c_y s_x s_y + 3 a_{10} c_y^2 s_x s_y + 2 a_5 c_x c_z s_x s_y + \\
 & 2 a_{11} c_y c_z s_x s_y + a_{13} c_z^2 s_x s_y + a_4 c_x^2 s_y^2 + 3 a_{10} c_x c_y s_y^2 + 6 a_{20} c_y^2 s_y^2 + a_{11} c_x c_z s_y^2 + \\
 & 3 a_{21} c_y c_z s_y^2 + a_{23} c_z^2 s_y^2 + a_8 c_x^2 s_z + a_{14} c_x c_y s_z + a_{24} c_y^2 s_z + 2 a_{17} c_x c_z s_z + 2 a_{27} c_y c_z s_z + \\
 & 3 a_{31} c_z^2 s_z + 3 a_2 c_x^2 s_x s_z + 2 a_5 c_x c_y s_x s_z + a_{11} c_y^2 s_x s_z + 4 a_7 c_x c_z s_x s_z + 2 a_{13} c_y c_z s_x s_z + \\
 & 3 a_{16} c_z^2 s_x s_z + a_5 c_x^2 s_y s_z + 2 a_{11} c_x c_y s_y s_z + 3 a_{21} c_y^2 s_y s_z + 2 a_{13} c_x c_z s_y s_z + 4 a_{23} c_y c_z s_y s_z + \\
 & 3 a_{26} c_z^2 s_y s_z + a_7 c_x^2 s_z^2 + a_{13} c_x c_y s_z^2 + a_{23} c_y^2 s_z^2 + 3 a_{16} c_x c_z s_z^2 + 3 a_{26} c_y c_z s_z^2 + 6 a_{30} c_z^2 s_z^2 L + \\
 & t H a_{19} c_x + a_{29} c_y + a_{33} c_z + 2 a_9 c_x s_x + a_{15} c_y s_x + a_{18} c_z s_x + 3 a_3 c_x s_x^2 + a_6 c_y s_x^2 + a_8 c_z s_x^2 + \\
 & 4 a_0 c_x s_x^3 + a_1 c_y s_x^3 + a_2 c_z s_x^3 + a_{15} c_x s_y + 2 a_{25} c_y s_y + a_{28} c_z s_y + 2 a_6 c_x s_x s_y + \\
 & 2 a_{12} c_y s_x s_y + a_{14} c_z s_x s_y + 3 a_1 c_x s_x^2 s_y + 2 a_4 c_y s_x^2 s_y + a_5 c_z s_x^2 s_y + a_{12} c_x s_y^2 + \\
 & 3 a_{22} c_y s_y^2 + a_{24} c_z s_y^2 + 2 a_4 c_x s_x s_y^2 + 3 a_{10} c_y s_x s_y^2 + a_{11} c_z s_x s_y^2 + a_{10} c_x s_y^3 + 4 a_{20} c_y s_y^3 + \\
 & a_{21} c_z s_y^3 + a_{18} c_x s_z + a_{28} c_y s_z + 2 a_{32} c_z s_z + 2 a_8 c_x s_x s_z + a_{14} c_y s_x s_z + 2 a_{17} c_z s_x s_z + \\
 & 3 a_2 c_x s_x s_z + a_5 c_y s_x s_z + 2 a_7 c_z s_x s_z + a_{14} c_x s_y s_z + 2 a_{24} c_y s_y s_z + 2 a_{27} c_z s_y s_z + \\
 & 2 a_5 c_x s_x s_y s_z + 2 a_{11} c_y s_x s_y s_z + 2 a_{13} c_z s_x s_y s_z + a_{11} c_x s_y^2 s_z + 3 a_{21} c_y s_y^2 s_z + \\
 & 2 a_{23} c_z s_y^2 s_z + a_{17} c_x s_z^2 + a_{27} c_y s_z^2 + 3 a_{31} c_z s_z^2 + 2 a_7 c_x s_x s_z^2 + a_{13} c_y s_x s_z^2 + 3 a_{16} c_z s_x s_z^2 + \\
 & a_{13} c_x s_y s_z^2 + 2 a_{23} c_y s_y s_z^2 + 3 a_{26} c_z s_y s_z^2 + a_{16} c_x s_z^3 + a_{26} c_y s_z^3 + 4 a_{30} c_z s_z^3 L
 \end{aligned}$$

In[3]:= **D@Quartic@x, y, zD, xD**

$$\begin{aligned}
 Out[3]= & 4 x^3 a_0 + 3 x^2 y a_1 + 3 x^2 z a_2 + 3 x^2 a_3 + 2 x y^2 a_4 + 2 x y z a_5 + 2 x y a_6 + 2 x z^2 a_7 + 2 x z a_8 + \\
 & 2 x a_9 + y^3 a_{10} + y^2 z a_{11} + y^2 a_{12} + y z^2 a_{13} + y z a_{14} + y a_{15} + z^3 a_{16} + z^2 a_{17} + z a_{18} + a_{19}
 \end{aligned}$$

In[4]:= **D@Quartic@x, y, zD, yD**

$$\begin{aligned}
 Out[4]= & x^3 a_1 + 2 x^2 y a_4 + x^2 z a_5 + x^2 a_6 + 3 x y^2 a_{10} + 2 x y z a_{11} + 2 x y a_{12} + x z^2 a_{13} + x z a_{14} + x a_{15} + \\
 & 4 y^3 a_{20} + 3 y^2 z a_{21} + 3 y^2 a_{22} + 2 y z^2 a_{23} + 2 y z a_{24} + 2 y a_{25} + z^3 a_{26} + z^2 a_{27} + z a_{28} + a_{29}
 \end{aligned}$$

In[5]:= **D@Quartic@x, y, zD, zD**

$$\begin{aligned}
 Out[5]= & x^3 a_2 + x^2 y a_5 + 2 x^2 z a_7 + x^2 a_8 + x y^2 a_{11} + 2 x y z a_{13} + x y a_{14} + 3 x z^2 a_{16} + 2 x z a_{17} + x a_{18} + \\
 & y^3 a_{21} + 2 y^2 z a_{23} + y^2 a_{24} + 3 y z^2 a_{26} + 2 y z a_{27} + y a_{28} + 4 z^3 a_{30} + 3 z^2 a_{31} + 2 z a_{32} + a_{33}
 \end{aligned}$$